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EVALUATION OF WORK DISTRIBUTION  
ALGORITHMS AND HARDWARE TOPOLOGIES IN A  
MULTI-TRANSPUTER NETWORK

by

William R. Cloughley

June 1988

Thesis Advisor:

Richard A. Adams

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Evaluation of Work Distribution Algorithms and Hardware  
Topologies in a Multi-Transputer Network

by

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Submitted in partial fulfillment of the  
requirements for the degree of

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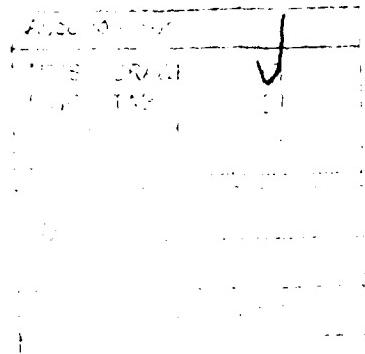
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## ABSTRACT

This thesis presents the evaluation of work distribution algorithms and hardware topologies in a multi-Transputer network. The primary emphasis concerns a work distribution algorithm known as "workfarm" that is effective on problems that are divisible into independent work packets.

All the programs and examples presented in this thesis were implemented in the OCCAM programming language, using the Transputer Development System, D700C, Beta 2.0 March 1987 compiler version.



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#### THESIS DISCLAIMER

The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

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INMOS limited, Bristol, United Kingdom

Transputer

OCCAM

IMS T414

IMS T800

Transputer Development System (TDS)

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#### DEDICATION

This thesis is dedicated to the following people: to my parents, for having instilled in me the desire to learn and to seek challenge; to LCDR Greg Bryant, whose brilliant thinking and willingness to help lifted the level of learning of the entire Transputer lab; to Major Richard Adams, whose professionalism and selfless dedication to teaching helped me and my classmates immeasurably; and most of all, to my lovely wife Lynnette, who cheered me up when things were not going well and made sure I did not rest on my laurels when I thought they were.

## I. INTRODUCTION

### A. BACKGROUND

The driving force behind modern weapon systems is the processor. At present, most weapon systems utilize a traditional single-CPU serial computer for their processing. Unfortunately, such a computer can process a certain amount of data in a fixed amount of time and no more. A modern radar or sonar can overwhelm the system processor with a flood of raw data. If only part of that data is processed, the rest is lost forever. A new, more powerful computer is required to handle more data. This thesis is part of an effort to improve the processing power of weapon systems.

Multiple computers working in parallel offer significant increases in processing power in a way that provides flexibility and expandability. If one needs more processing power, one adds more computers.

The biggest problem in parallel multi-computer networks is interprocessor communication. This communication is usually handled in one of two ways. The traditional method has been to connect multiple computers together by way of a shared bus. The computers communicate by leaving messages in a single shared memory. The shared memory and shared bus create bottlenecks, however. Memory also creates a bottleneck, since bus bandwidth is higher than memory bandwidth.

The number of computers that can be attached is limited by the bus bandwidth and/or memory bandwidth. A second approach is to have computers communicate with each other by passing messages along direct links. In such systems, each computer has its own memory.

This thesis concentrates on the latter method, since it is attractive for use in a weapon system for reasons of flexibility, growth potential, fault tolerance, lower costs, better response time, and higher system availability.

Microprocessors would seem well suited for a parallel multi-computer network in a weapon system as they are inexpensive, small, lightweight, and increasingly powerful. Until now, however, microprocessors were designed to operate as stand alone computers. Parallelism, with its requirement for communication between computers, was a difficult problem. Since they were not originally intended for this role, their architectures were not suited for it. If they had any provisions for communications at all, they were added on as an afterthought.

A microprocessor family called the Transputer, designed from the ground up for parallelism, is now available from INMOS corporation. It features four full duplex serial communication links and a language also specifically designed for parallel processing. The Transputer is ideal as a building block for a parallel system of microprocessors.

Obviously the evaluation of any computer system, be it single or multi-processor, depends upon the problem. This thesis evaluates a network of Transputers working on a problem that can be broken up into independent work packets. Each packet contains parameters required to process part of the problem. Packets may be combined into a bundle to make communications between nodes more efficient. The amount of computation per packet may be very small or very large and may vary depending on the particular packet.

A critical part of any parallel multi-computer network is the work distribution algorithm. Such an algorithm known as the Workfarm is simple and very effective for many problems including Ray Tracing and Mandelbrot Set and is used in this thesis [MaSh87].

With four links on each Transputer, many physical topologies for a network are possible. To make communication and configuration software less complex, a very regular and symmetric topology is often desirable. There are many such topologies available, from a simple linear array or binary tree to more exotic designs like hypercube or hypernet [HwGh87].

The time it takes for a network of Transputer to complete a problem using a workfarm is primarily dependent on the following factors: the number and speed of the Transputers, the number of computations per packet, the number of

packets per bundle, and the total number of packets in the problem.

This thesis will examine how these factors are interrelated. The two primary questions addressed are, given a workfarm, 1) how many Transputers will be required to solve a problem given a time limit, and 2) how fast can a problem be solved for a given number of Transputers?

The resulting predictions will be compared to actual results on two specific problems: Mandelbrot Set [Po86] and Coordinate Transformation [Ri87]. These problems can be characterized by their divisibility into work packets which can be processed in any order and by their massive computational requirements.

#### B. THESIS OVERVIEW

Chapter II presents a brief look at the Transputer system. Chapter III discusses the workfarm, how it is implemented on a network of Transputers, and what topology is used. Chapter IV presents the results of timing studies using the workfarm. Chapter V uses the findings of Chapter IV to predict the performance of the Coordinate Transformation and Mandelbrot Set problems and compares them with the actual results. Chapter VI presents the conclusions and recommendations of the thesis.

## II. THE SYSTEM

### A. GENERAL

It is hard to separate the Transputer hardware and Occam software. They are so tightly intertwined that it is easier to treat them as a single entity; the Transputer system. A basic understanding of this system is necessary when programming a network of Transputers. Although this learning may seem onerous, it may well be the reason Transputers are relatively easy to program in parallel compared with other microprocessors and languages. The reader is assumed to be familiar with the fundamentals of the Transputer architecture and the Occam programming language. For those unfamiliar with Transputers, [In88] and [PoMa87] are excellent starting points. This chapter highlights the knowledge necessary for efficient parallel processing and performance maximization.

Despite a network of Transputers's tremendous power, a program has to be as efficient as possible to realize the full potential. To do so, the programmer must first ensure that each individual Transputer is optimized and then that the network is. The latter is primarily a matter of work distribution and communication. The following is a synopsis of Transputer performance maximization; a complete reference can be found in [At87].

## B. SINGLE TRANSPUTER OPTIMIZATION

It is extremely desirable to keep all the data structures and code in the on-chip memory. An on-chip memory cycle takes one processor cycle (50 nanoseconds for the latest 20MHz Transputers). Although variable, depending on the instruction and on the speed of the DRAM chips, external memory references usually take five processor cycles [In87a]. In other words, one external memory access takes five times as long as an on-chip memory access.

Given a choice between data structures on-chip or program code on-chip but not both, one would choose data structures. A Transputer word holds four bytes; one memory access of program code returns four single byte instructions. That, combined with the principle of locality, means accessing program instructions from external memory is not nearly as slow as accessing data structures from external memory.

Transputer memory is arranged as follows, from the base of memory upwards: system space, data space, code space, with any unused space on top. Off chip (external) memory is not allotted until there is no free on-chip memory remaining. The Occam compiler and Transputer loader software automatically places data (data structures, workspaces, etc.) lower than program code on the Occam map [At87]; hence, program code only resides in on-chip memory if the data space has already been accommodated.

The programmer has control over the order in which data structures occur in memory through the order in which they are declared in the code. Simply put, data structures declared last in a local block are placed lower in the memory map than their predecessors.

Large data structures, such as arrays, should be declared first in a local block, followed by any variables, so that the variables are allotted memory lower in the map, ahead of the large arrays. Otherwise, frequently used variables may be allotted off chip memory. To ensure large data structures do not monopolize on-chip memory, they can be declared in a global process. In keeping with proper programming practices, i.e., declaring data structures locally, the global data structures can be artificially declared locally using abbreviations with no performance cost.

Concurrent process workspaces also reside in the data portion of the memory map. The programmer controls which processes lie lower in the memory map by the order in which they are declared. Like data structures, those processes declared last are allotted workspaces lower in the memory map.

To finetune the Transputer further, awareness of where variables lie relative to the workspace pointer is useful. Only a single byte instruction is required to manipulate the first 16 locations above the workspace pointer because the four bit relative address fits in the lower half of the

single byte instruction. This optimization is technique is useful in a local block with more than 16 variables.

### C. MULTIPLE TRANSPUTER OPTIMIZATION

A key to maximizing the performance of a network of Transputers is decoupling communication from calculation. This is accomplished by running communication and calculation processes separately and in parallel. Other processes, also running in parallel, act as buffers between the communication and calculation processes. The processes communicate among themselves through internal or external channels. With such a setup, a Transputer may now communicate and calculate simultaneously, with little degradation in either area.

Equally important, the communication processes must always run at high priority and the calculation processes at low priority. Consider a network of Transputers. If each Transputer only passes messages when finished its own calculation, the majority of the Transputers in the network will constantly lie idle, waiting to receive work or to send results. The communication must take precedence so that the message passing is uninhibited.

Because the communication and calculation are decoupled in each Transputer, the communication does not significantly affect the ongoing calculation. How much calculation degradation actually occurs during ongoing communication was researched in [Ha87] and [Br88]. In a nutshell, a single

Transputer communicating on all four links at full capacity, which is the worst case scenario, can still calculate at approximately 75% of its maximum capability [Ha87]. The separate DMA engines on the chip make this possible, although the degradation is caused by internal bus contention between the link engines and the central processor.

The actual link data rates have been investigated previously in [Va87] and [Br88]. To summarize, one can expect rates of approximately 2.3 Mbytes/second through T800 links during bidirectional communication and 1.7 Mbytes/second during unidirectional communication. The T414 has rates of 1.5 Mbytes/second during bidirectional communication and 0.76 Mbytes/second during unidirectional communication [Br88]. These rates assume no external memory usage. The T800 communicates significantly faster than the T414 because of a handshaking improvement in link communication [In87b].

A third area in which a programmer can significantly affect performance is the length of the communication message. The overhead to send a single integer over a link is the same as that to send an array of 100 integers, for example. Obviously it is better to keep messages as long as possible and cut down on the overhead.

As the message length grows, however, the probability increases that its data structure will reside in off chip memory. That of course means significant performance degradation.

The trick is to keep the message as long as possible without going into off chip memory. The programmer can figure out the happy medium by keeping track of how much data structure space he is using and making sure it is less than the on-chip memory size. If it is more, the programmer has to shorten his message arrays until all the data structures fit in on-chip memory.

#### D. MISCELLANEOUS TIPS

As pointed out in [Br88], the timer should not be utilized in the B004 T414 Transputer. It does not return an accurate measure of time because the T414 is executing processes that the user is not aware of and these hidden processes figure into any timing measurements. The timer should be utilized on a remote Transputer and the time returned over a link for display.

Occam is very strongly typed. In a network of Transputers, where message passing is paramount, this comes heavily into play. The type of data at one end of a channel must be the same type that comes out the other end or the program deadlocks. This error is particularly insidious because there is always a lot of communication in a network and there are no messages to tell why the program has stopped. For this reason, it is imperative to begin testing on a B004, followed by testing on a single remote Transputer, before testing a program on a network of Transputers.

Protocols are used to identify what is coming across a channel; however, only data of that protocol will be able to use the channel. A more flexible approach is use of the CHAN OF ANY declaration which allows the programmer to send anything down a channel as long as the same thing comes out the other end.

Variant protocols offer the same flexibility. They are expensive in terms of overhead, however. A cheaper but trickier method is to declare channels using CHAN OF ANY and sending arrays through these channels with a single byte or integer tag at the head. The tag allows the receiver to know what type of data follows in the array. This manual method requires retyping, a practice requiring much care from the programmer, and should be well tested on a single remote Transputer before it is used in a network.

All Transputer links may run at the standard speed of 10 Mbits/second; however, most members of the Transputer family are now capable of running their links at 20 Mbits/second. The B004, B002, and B001 are the only commonly used boards restricted to the standard link speed. Fortunately, the 20 Mbits/second capable boards allow their Link Os to be set at 10 Mbits/second while the rest of the links run at 20 Mbits/second for fastest communications except where an input is accepted from a B004 host computer or B001/2 RS232 interface board. It is easy to tell if the DIP switches have

been improperly set; an error message will flash when the extracted code will not load through the mismatched link.

#### E. DEBUGGING

The Transputer's internal architecture time slices parallel processes to simulate parallel processing. This aids the programmer because he can test his program on one Transputer; then, with minimal change, run his program on a network of Transputers as intended.

Based on programming experiences, it is recommended that a program intended for a network of Transputers be developed in three steps. First, the calculation process is tested sequentially on the B004 T414 Transputer. The B004's host computer allows the programmer to easily display any variables in the executing program.

The next step is to run the same program on a remote Transputer connected to the B004. Any bugs with the external links or channel protocols will reveal themselves in this step. Because a program may work on one Transputer using internal channels but not on multiple Transputers using external channels, this step is important. During execution, variables may be passed over external links back to the B004 for display.

Finally, the program is run on a network of Transputers. There may still be bugs but at least the programmer knows that a large portion of his code is good, especially the channel protocols. The first two testing systems remain and

the programmer can reuse them to check out any questions he may have.

The problem is that in a network of Transputers a program either works or it deadlocks. When a program deadlocks, all the programmer sees is a blinking cursor. There is very little the programmer can do to determine what went wrong, where the problem occurred, or to obtain a state trace. Additionally, because the Transputers run in parallel, it is next to impossible to display variables to a monitor during execution.

### III. THE WORKFARM

#### A. GENERAL

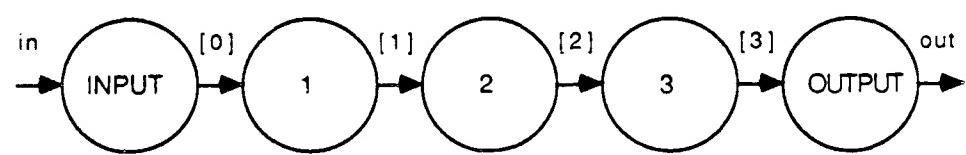
A problem has to be divisible for use in a parallel system. A parallel system of Transputers is so powerful that the problem should also be computation intensive. This thesis deals with problems that are both divisible and computation intensive. Problems that are not divisible (assuming a single input data stream) are not germane to this thesis.

#### B. PIPELINE

The pipeline is a well known work distribution algorithm. It is ideal for problems that divide into tasks that can be assigned to separate processors. With the Occam programming language and the Transputer links, it is easy to configure a network of Transputers into a pipeline, as demonstrated in Figures 3.1 and 3.2.

Unfortunately, pipelines are only as fast as their slowest process. In a pipeline, the Transputers execute the following cycle:

```
WHILE TRUE
  SEQ
    communicate
    synchronize
    calculate
    synchronize.
```



---

Figure 3.1  
Transputer Pipeline

---

```
[4]CHAN OF ANY chan:  
PAR  
    input  (in,      chan[0])  
    proc1 (chan[0],  chan[1])  
    proc2 (chan[1],  chan[2])  
    proc3 (chan[2],  chan[3])  
    output (chan[3], out)
```

---

Figure 3.2  
Transputer Pipeline Code

To maximize performance, the calculation time of the processes must be equal. This limits the problem range.

A special case is when each processor in a pipeline can do the same task. Heat transfer along a wire is such a problem, although in this case the pipeline is bidirectional. The calculation time for each processor is equal and so the network can achieve peak efficiency. The configuration for this special pipeline, as demonstrated in Figures 3.3 and 3.4, is even simpler than that of the standard pipeline.

#### C. WORKFARM

The workfarm is a work distribution algorithm in which each processor does the same task on part of a problem instead of each processor doing a separate task as in the standard pipeline. It is highly effective on problems that can be divided up into independent work packets, where each packet consists of parameters necessary to calculate a part of the problem. Independent means that no packet is dependent on any others. If one packet of the total were lost, only a small piece of the problem would be missing. The amount of work required per packet may vary.

The workfarm has two distinct parts: the Controller and the Farm. The controller combines packets into request bundles and passes the request bundles to the farm, ensuring that there are never more bundles in the farm than the farm can handle. The controller also receives the result bundles.

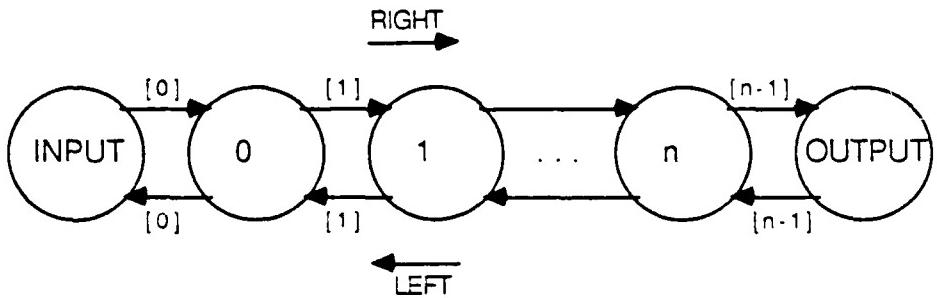


Figure 3.3  
Bidirectional Pipeline

---

```
[num.nodes+1]CHAN OF ANY right, left:  
SEQ  
    input (right[0], left[0])  
    PAR i = 0 FOR num.nodes  
        node (right[i], right[i+1],  
              left[i+1], left[i])  
    output (right[num.nodes], left[num.nodes])
```

---

Figure 3.4  
Bidirectional Pipeline Code

The packets are grouped into bundles to optimize the length of the message arrays as discussed earlier.

The farm consists of multiple nodes arranged in some topology. This thesis uses a linear array of nodes for reasons explained later. A workfarm of this type is pictured in Figure 3.5.

When a node receives a request bundle and is not "busy" it accepts the new one for processing. However, if the node is busy when the request bundle arrives, it passes the bundle to the next node (further away from the controller). Result bundles, arriving from the opposite direction, are simply passed along to the next node until they reach the controller. When a node finishes processing a bundle, it sends its result bundle towards the controller.

In the workfarm, each node has the same code, although sometimes it may be desirable to make minor modifications to the end node code.

The configuration code for a workfarm is listed in Figure 3.6. Two arrays of channels are declared, one to carry the request bundles out to the farm and the other to return the result bundles back to the controller. Expanding the farm of Transputers is as easy as changing the constant 'num.Transputers'. Note that the controller and node processes each have been "placed" on a separate Transputer, in this case a T414 controller and T800 nodes.

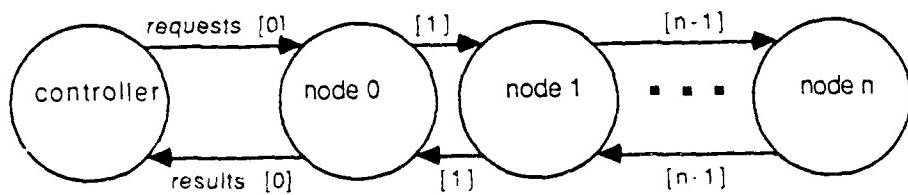


Figure 3.5

Linear Array Workfarm

```

[num.Transputers]CHAN OF ANY requests, results:
PLACED PAR
    PROCESSOR T4 100
        controller (requests[0], results[0])
    PLACED PAR i = 0 FOR num.Transputers
        PROCESSOR T8 i
            node (requests[i], requests[i+1],
                  results[i+1], results[i])

```

Figure 3.6

Linear Array Workfarm Code

The controller consists of four processes running in parallel as shown in Figures 3.7 and 3.8. Requests and results are external channels passed in by the global configuration process; all other channels are internal to the controller and must be declared.

The generator initiates the entire workfarm process by creating the request bundles and passing them to the work router. If necessary, the generator may receive inputs from outside sources through external channels to build the packets and bundles. The generator signals the handler just before it begins to pass out bundles and is in turn signalled by the handler when the handler has received the last result bundle.

The work router and result router are essentially buffer processes. Together, they also perform a vital valve function to make sure the farm never exceeds its capacity for request bundles. The work router knows how many nodes are in the farm. Since each node has a buffer enabling it to hold two bundles at a time, the work router knows the farm can hold twice as many request bundles as the number of nodes. It was necessary to reduce by one the farm bundle capacity known to the work router to avoid overloading the farm.

When the work router passes a bundle to the farm, it increments a counter. When the results router receives a bundle, it signals the work router through the trigger channel. When the work router is signaled, it decrements the

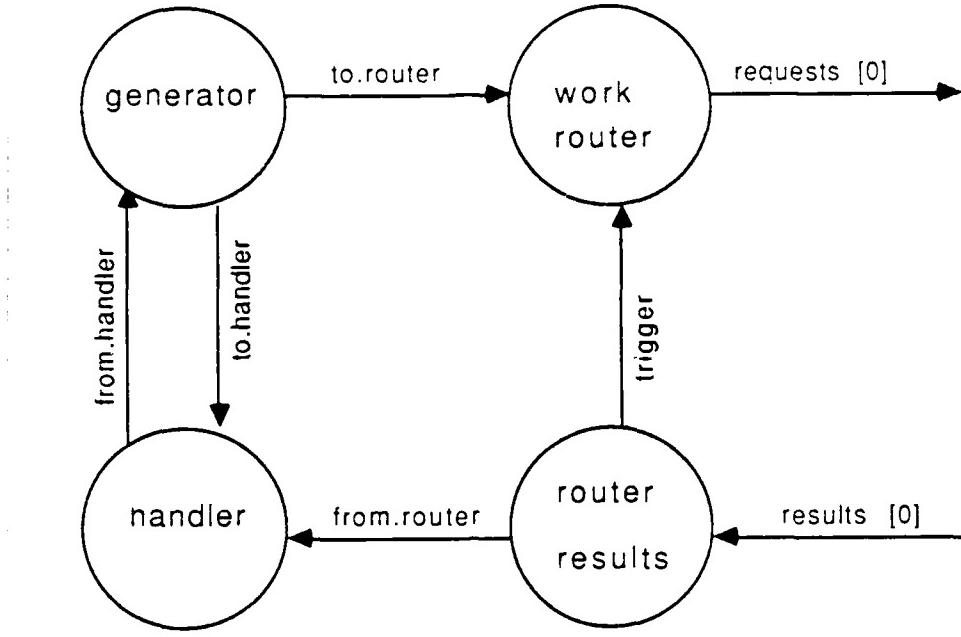


Figure 3.7

The Controller

---

```

CHAN OF ANY to.router, from.router:
CHAN OF ANY to.handler, from.handler:
CHAN OF ANY trigger:
PAR
    generator (to.router, to.handler, from.handler)
    work.router (to.router, trigger, requests)
    results.router (from.router, trigger, results)
    handler (from.router, to.handler, from.handler)

```

---

Figure 3.8

Controller Code

counter. The work router will only accept bundles from the generator while the counter does not exceed the farm bundle capacity. The code to implement this valve function is shown in Figure 3.9.

When the handler receives the last of the result bundles it signals the generator that the problem has been completed.

```
--- Work.router
VAL    farm.capacity IS (num.Transputers * 2) - 1:
BOOL   bundle.done:
INT    count:
SFC
    count := 0
    WHILE TRUE
        PRI ALT
            trigger ? bundle.done
            count := count - 1
            (count <= farm.capacity) & to.router ? bundle
                SEQ
                    requests ! bundle
                    count := count + 1

--- Results.router
VAL    bundle.done IS TRUE:
WHILE TRUE
    SEQ
        results ? bundle
    PAR
        trigger ! bundle.done
        to.handler ! bundle
```

Figure 3.9

Valve Function Code

A single node on the farm consists of five processes: a work router, a result router, a work buffer, a result buffer, and a calculation process. A single node is shown in

Figures 3.10 and 3.11. Notice that the calculation process is given low priority while the four communication processes run at high priority, as explained in Chapter II.

```
CHAN OF ANY    to.buffer, to.calculation:  
CHAN OF ANY    from.calculation, from.buffer:  
CHAN OF BOOL   signal:  
PRI PAR  
PAR  
    work.router (requests.in, requests.out,  
                  to.buffer, signal)  
    work.buffer (to.buffer, to.calculation)  
    result.buffer (from.calculation, from.buffer)  
    result.router (from.buffer, results.in, results.out)  
    calculation (to.calculation, from.calculation)
```

Figure 3.10

Single Node Code

The work router accepts bundles from the requests-in channel. If the work buffer is full, the work router relays the bundle to the next node in line by way of the requests-out channel. If the work buffer is empty, the bundle is sent there and the work buffer full flag is set.

The work and result buffers are present to decouple the communication in the work and result router processes from the calculation in the calculation process, as explained in Chapter II.

The work buffer holds a single bundle at a time. When the calculation process accepts a bundle from the work buffer, the work buffer signals the work router that the buffer is empty.

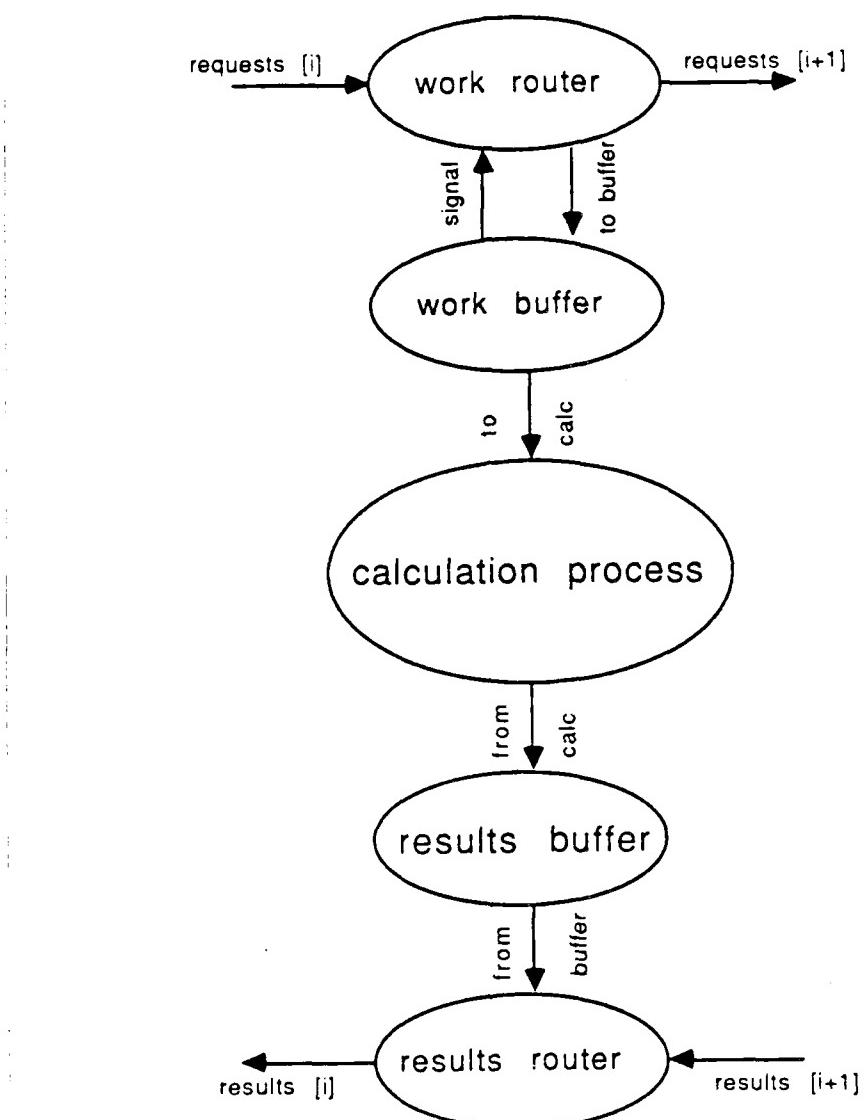


Figure 3.11

Single Node

The calculation process is where all work occurs. There, upon arrival, a bundle is separated into packets. The packets are processed sequentially and the results grouped into a result bundle. After the result bundle has been passed to the result buffer, the calculation process is ready to accept another bundle. Since the calculation process is sequential, it could be coded in a programming language other than OCCAM such as Ada, Pascal, or C and inserted into the OCCAM workfarm harness.

The results buffer is a pure buffer that relays a result bundle to the result handler and waits for another result bundle to arrive.

The results router receives result bundles either from the result buffer or the results-in external channel. In either case, the bundle is discharged along the results-out channel. An arriving bundle from the buffer is given priority over the external channel so that the calculation process will be free for more work as soon as possible.

There has to be some device to allow for matters of initialization and reporting in the farm. The method used in this thesis was to place a tag at the head of every bundle array. Depending on the tag, a bundle could be of the following types: setup, data, or report. Generally, upon arrival of a bundle, the tag is examined, and action is taken on the bundle accordingly.

#### D. TOPOLOGY

A workfarm is not limited to the linear array; trees are an attractive option. Because of communication path lengths, trees would seem better suited for a workfarm with large numbers of Transputers. Consider linear array and binary tree workfarms, each with 100 farm nodes, for example. Assuming the problem was computation intensive enough so that all 100 nodes would be utilized, a bundle would have to travel through 99 nodes to get to the 100th node in the linear array. In the binary tree, however, a bundle would have to travel through at most six nodes to reach any of the 100 nodes. A trinary tree would lower the communication overhead further. Given a workfarm of the same number of Transputers working the same problem, trees are more efficient than linear array in terms of utilizing each Transputer.

Trees were not used in the research for a number of reasons, however. First of all, there were not enough Transputers available to conduct research and achieve significant results. A binary tree workfarm was implemented but the performance gains were so minuscule that the author believes that significant gains would not be realized until large numbers of Transputers, perhaps 50 or more, were used. The modification to the linear array workfarm algorithm to achieve binary tree topology was slight and only occurred in the work and result routing processes of the node process.

The actual code is listed in Appendix A. Secondly, the B003 boards, with four Transputers each, are not well suited to implementing trees since half of the 16 links are hardwired.

A large number of processors must be arranged in a regular fashion or the configuration code and communication algorithms become too complex. Commonly used regular structures are arrays (1D, 2D, 3D, ...), trees (binary, trinary, etc.), and hypercubes. More complex but still regular structures have been proposed such as hypernet [HwGh87]. Such structures appear promising for a networks of large numbers of Transputers.

#### IV. WORKFARM PERFORMANCE

##### A. GENERAL

The performance of a workfarm is dependent on the following factors: the number and speed of the Transputers, the number of packets in the problem, the number of computations per packet, the packet size, and the number of packets per bundle. To determine the relationships between these factors and ultimately the number of Transputers required to complete a problem in a certain amount of time, research was conducted on a standard workfarm using a variable problem.

##### B. ENVIRONMENT

The research in this chapter was conducted on a workfarm with a physical configuration as pictured in Figure 4.1. The number of Transputers utilized in the farm portion was varied from one to eight. The speed of an individual Transputer depended on its respective type. The controller process was placed on a remote T414-15 Transputer. The T414 on the B004 board was used only for the compiling, extraction, and loading of code to the workfarm network. The farm nodes were placed on T800 Transputers.

A B002 board with its T414-15 and RS232 interface was utilized so that results could be displayed to a VT220 terminal. The B007 board was included in the network for any

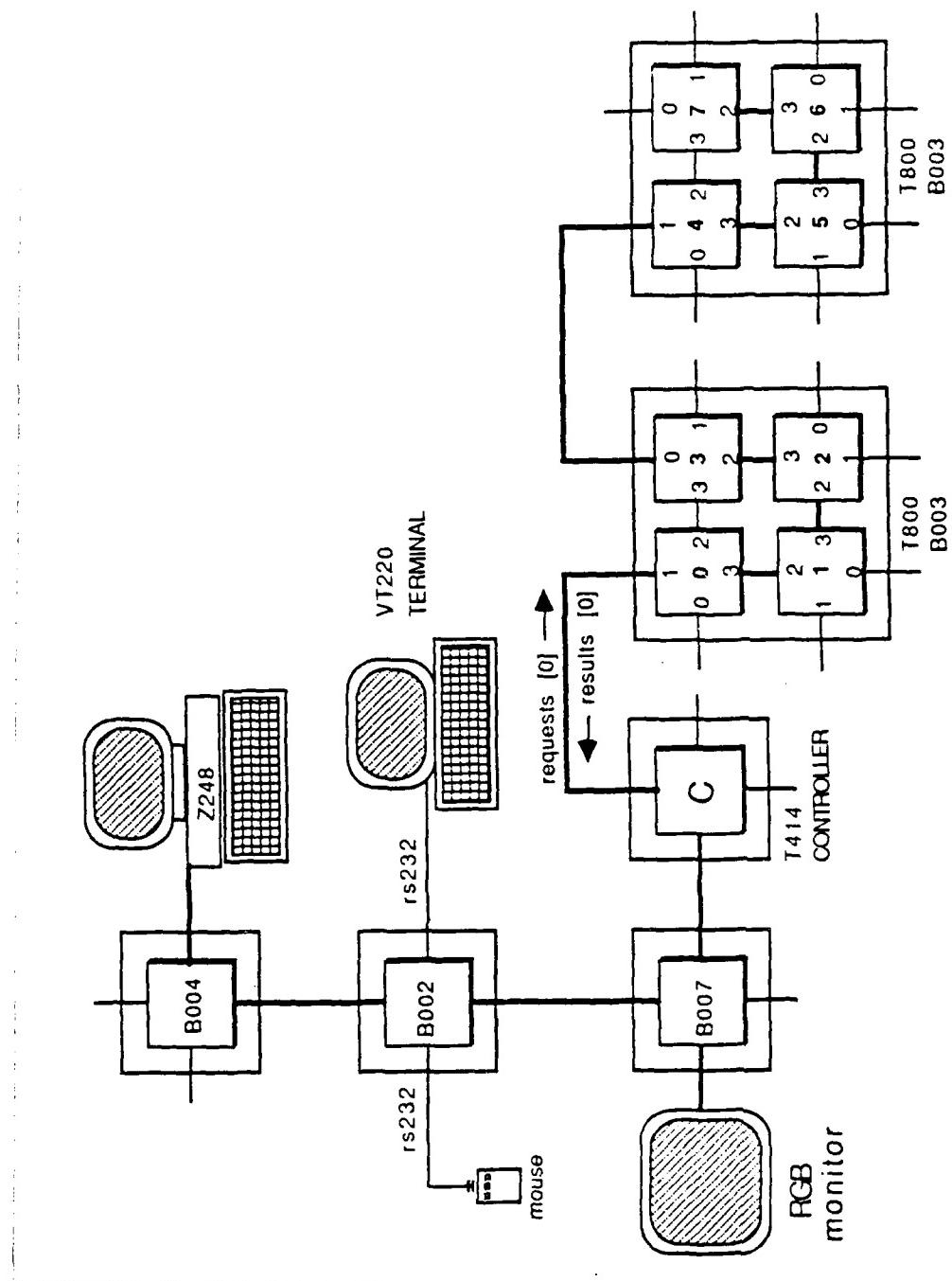


Figure 4.1

Workfarm Physical Configuration

future graphic work. It acted solely as a relay and did not figure in any of the testing. The entire workfarm network ran at a common link speed of 20 Mbits/second except for the B004 and B002 boards.

### C. TESTING APPARATUS

To change problems on a workfarm requires modification of the calculation process of the farm nodes, the generator process, the handler process, and the message arrays that pass throughout the farm. To test the workfarm, it was necessary to be able to vary the problem size quickly and easily. The problem consisted of a variable number of 32 bit floating point (REAL32) multiplications and the constant communication overhead of the workfarm algorithm. When the farm nodes were initialized, each farm node was passed an integer representing a certain number of calculations per packet.

The generator process produced a certain number of packets which were grouped into bundles and distributed to the farm, as shown in Figure 4.2. When a calculation process in the farm received a bundle, it simulated separating the packets from the bundle and did "calculation.per.packets" REAL32 multiplications. The calculation process simulated assembling a result bundle and was then ready for the next bundle. This testing calculation process is shown in Figure 4.3.

```
tag := data
SEQ i = 0 for total.bundles
SEQ
    SEQ j = 1 FOR packets.per.bundle
        [bundle FROM (j TIMES 4) FOR 4] :=
            [dummy.array FROM 0 FOR 4]
    requests ! bundle
```

Figure 4.2  
Generator Process Code

```
SEQ i = 1 FOR packets.per.bundle
SEQ
    [dummy.array FROM 0 FOR 4] :=
        [bundle.in FROM (i TIMES 4) FOR 4]
    SEQ j = 0 FOR calcs.per.packet
        x := x*x
    SEQ j = 0 FOR 4
        bundle.out [j] := dummy(BYTE)
```

Figure 4.3  
Calculation Process Code

A timer was started preceding the initialization phase. When the handler process received the last result bundle the problem was completed and the timer was stopped. The time required to complete the entire problem was simply the stop time minus the start time.

During the report phase, the handler received packets from the farm nodes that contained the number of bundles that each node processed and the node identification. The handler passed this information and the problem completion time to the VT220 terminal for display.

The bundle used for communication in the workfarm consisted of an array of bytes. The first four bytes were retyped to represent the integer tag. The next eight bytes were retyped into a setup array of two integers to hold initialization values. When the bundles were used in their normal role of carrying packets, they were essentially "dummy" arrays, as the only meaningful information in each bundle was the tag. Figure 4.4 lists the bundle declaration.

---

```
VAL packets.per.bundle IS 10000/total.bundles:  
VAL bundle.size      IS packets.per.bundle + 1:  
VAL packet.size.int  IS 1:  
VAL bundle.size.byte IS bundle.size.int TIMES 4:  
VAL packet.size.byte IS packet.size.int TIMES 4:  
  
[bundle.size]BYTE      bundle:  
INT    tag             RETYPES [bundle FROM 0 FOR 4]:  
[]INT   setup.array     RETYPES [bundle FRCM 4 FOR 8]:
```

---

Figure 4.4

Bundle Declaration

The packet size used for the research was one integer. This represented a unit packet with four byte-size parameters. Most problems will have packets consisting of some multiple of four bytes; for example, the Mandelbrot Set problem has 12 byte request packets and 32 byte result packets.

#### D. RESULTS AND CONCLUSIONS

Figure 4.5 illustrates some of the relationships that exist in an eight Transputer workfarm among the many variables that affect performance. The vertical axis shows the time to calculate 10,000 packets. The horizontal axis indicates the number of REAL32 multiplications each packet represents. If calculations.per.packet is 100, the total workload is 1,000,000 REAL32 multiplications.

Each line of the graph represents a different bundle size, in terms of packets per bundle. For example, a bundle made up of 16 packets is 17 integers long (68 bytes): 16 one integer packets and a one integer tag.

Each line begins flat and at some point begins increasing linearly. The flat line indicates two things. While the line is flat, not all eight Transputers are being utilized. For small bundles of one packet per bundle, the farm is underutilized until the workload reaches 120 calculations per packet. As the bundle size increases, more Transputers are utilized sooner. For example, at 16 packets per bundle,

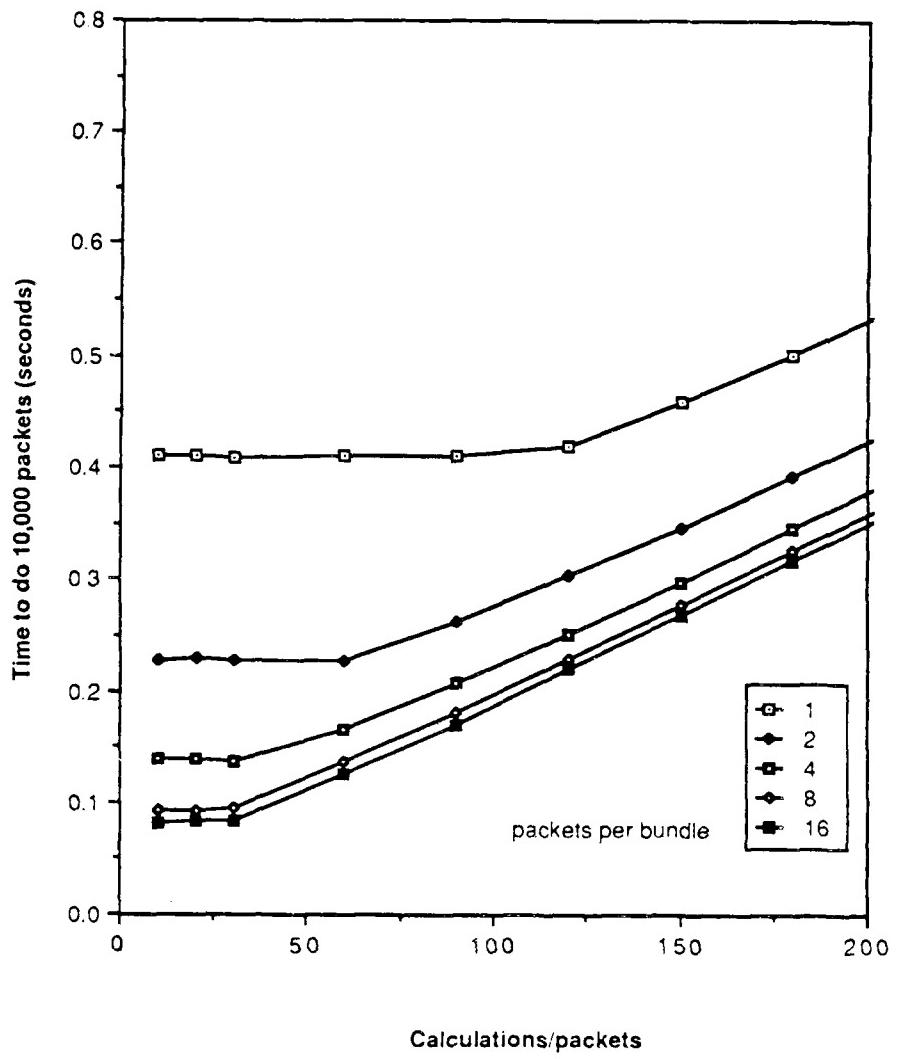


Figure 4.5  
Workfarm Performance Characteristics

the workfarm is fully utilized at approximately 30 calculations per packet.

The flat line also means that the workfarm is completing an increasing number of calculations with no corresponding increase in time. This is explained by observing how many Transputers were utilized at each calculation point. As the workload increased, the workfarm utilized more of its available processors. Of course, there came a time when all available Transputers, in this case eight, were in use. From then on, the time required increased proportionally to the increase in the workload.

Once all the farm Transputers were in use, and the workload continued increasing, the time increased at a constant rate. This rate was equal for all bundle sizes.

The question of time to complete a problem can best be represented by the following equation:

```
time := (calcs.per.packet * total.packets) + comm.ovhd
```

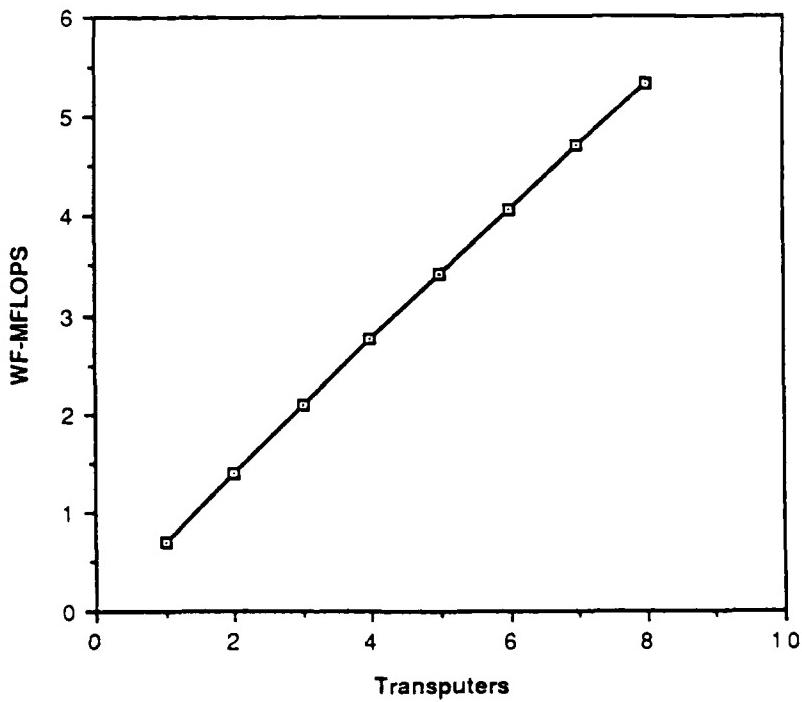
With a small number of calculations per packets, the communication overhead is a significant factor in the equation. As the workload increases, the communication overhead decreases in significance.

The time required to complete the problem decreased as the bundle size grew. At greater than 16 packets per bundle, however, the time reductions became negligible. This was not surprising, considering that with one packet per bundle,

half of the bundle was used for communication overhead (one integer for the tag, one integer for the packet). At 16 packets per bundle, however, 1/17 of the bundle was overhead, or 5.9 percent. Between one packet per bundle and 16 packets per bundle there was a large difference in the overhead percentage; the reductions in time was correspondingly great. The overhead percentage difference between 16 and 32 packets per bundle was small, however, and the reduction in time required was also correspondingly small.

In each farm node process, one bundle is declared in each of the four communication processes and two bundles are declared (bundle.in and bundle.out) in the calculation process. Sixteen packets per bundle (17 integers) is a good bundle size since the bundle is large enough to yield near optimal performance yet small enough to require little on-chip memory. Bundle sizes greater than 667 bytes will leave no room on the T800 on-chip memory for any other data structures because six bundle arrays will require 4002 bytes of memory which is close to the T800 on-chip memory capacity of 4096.

With 100 calculations per packet and 10,000 packets, the total workload is 1,000,000 REAL32 multiplications plus the communication overhead. Dividing the workload by the total time to complete the workload yields "workfarm mega-floating point operations per second" (WF-MFLOPS). Plotting WF-MFLOPS versus number of Transputers yields the graph in Figure 4.6.



---

Figure 4.6

Linear Performance

The resulting nearly straight line indicates that the workfarm is achieving near linear performance; that is to say, WF-MFLOPS is directly proportional to the number of Transputers in the farm.

It should be realized that at some number of Transputers, the line in Figure 4.6 will turn sharply horizontal. Where on the graph this occurs depends on the workload and number of Transputers. It represents the point at which the controller cannot provide request bundles fast enough to

keep all the farm nodes busy. Adding more Transputers to the farm beyond this point is wasteful, since no further increase in work capacity can ever occur.

It would be helpful to be able to predict either how many Transputers in a farm are needed to solve a problem in a certain amount of time or how long a problem will take given a certain number of farm Transputers. To do so, one has to realize that a workfarm can be in one of two limiting conditions, depending on the workload and number of Transputers. The first case is when the workfarm is "calculation limited"; that is, the ultimate performance is limited by the workload, not by the controller request bundle generation rate. The second case is when the workfarm is "communication limited"; with small workloads, the farm nodes are able to complete request bundles faster than the controller can supply them.

The workfarm performance can be characterized by a set of equations using the notation in Table 4.1. Figure 4.7 is provided as a reference.

The time to solve a problem on a workfarm ( $T$ ) is obviously

$$T = \frac{N}{r}.$$

And, since  $r \leq m$ ,

$$T = \frac{N}{r} \geq \frac{N}{m}.$$

TABLE 4.1  
WORKFARM VARIABLES

Variable	Represents
B	single node maximum calculation rate - bundles/second with no degradation
r	controller limiting rate - bundles/second
m	controller maximum rate - bundles/second
$a_i$	bundles/second accepted by node i for calculation
T	time to solve complete problem
N	total number of bundles in problem
n	total number of nodes in farm
$D_x$	degradation of B caused by x bundles/second

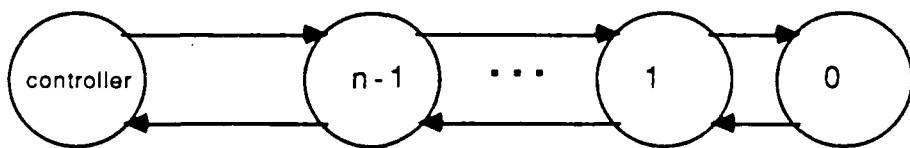


Figure 4.7

Workfarm Reference

With  $n$  farm nodes, each node accepts the following number of bundles per second for calculation:

$$a_0 = B$$

$$a_1 = B \cdot D_{a_0}$$

$$a_2 = B \cdot D_{a_0+a_1}$$

.

.

.

$$a_{n-1} = B \cdot D_{a_0+a_1+\dots+a_{n-2}}.$$

Thus,

$$m \geq r = \sum_{i=0}^{n-1} a_i.$$

The total number of bundles ( $N$ ) in a problem is a known factor that can be used for predictions. The rate that bundles can be accepted and processed by a single Transputer node without degradation ( $B$ ) can also be determined beforehand by measuring the maximum number of bundles that a single farm Transputer can process in a certain time period.

Consider the calculation limited workfarm, which is characterized by a large workload. There are two predictions that can be made. First of all, if there is a certain number of Transputers available, one can determine how long it will take to complete the problem. Secondly, if one has a time limit in which to complete the problem, one can determine

how many Transputers will be required, assuming the problem does not become controller limited.

Research showed that when the farm was calculation limited, each farm node processed approximately the same number of bundles, with a slight increase in processed bundles from first to last node. This corresponds to the decreasing degradation in the farm as the nodes further from the controller have to route less and less bundles. If the number of Transputers ( $n$ ) is known, and relatively few Transputers are used, the number of bundles processed by each farm node is approximately  $N/n$  or  $N_i$ . Since  $a_i$  is approximately the same for each node (discounting degradation) and the farm is calculation intensive, the overall time required by one node to complete  $N_i$  bundles can be assumed to be approximately the same as the overall time taken to complete the entire problem. This simple method to predict the overall time of a computation limited workfarm was effective to within five percent of the actual results. The resulting equation is:

$$T = \frac{N}{n \cdot B}.$$

To complete the problem in a given amount of time, one can calculate approximately how many Transputers will be required by merely switching  $T$  and  $n$  in the above equation:

$$n = \frac{N}{T \cdot B}.$$

The communication limited case is characterized by a low workload with the farm nodes accepting request bundles at a greater rate than in the calculation limited case. Obviously, the more request bundles accepted, the more result bundles generated; and in general, a greater percentage of processor time is spent passing bundles. The lower the workload, the sooner the farm will be able to exceed the controller's ability to supply bundles. If the first few farm nodes can match the rate at which the request bundles come from the controller, then nodes further down the line in the farm simply will not receive any work. Thus, the controller generation rate becomes the limiting factor as  $r$  decreases from  $m$ . This generation rate includes the overhead caused by the controller having to accept incoming result bundles. The number of nodes in the farm that do useful work is dependent on the capacity of the controller to supply request bundles.

It would be useful to know at what point a particular problem becomes communication limited; that is, for any problem, what is the maximum number of nodes in the farm that will do useful work. The workload and total number of bundles are known from the problem description. A rough estimation may be reached by assuming that at equilibrium, where some number of farm nodes are able to match the controller's request bundle generation rate ( $r$ ), each working node is processing approximately the same number of bundles. Dividing  $r$  by the single node maximum calculation rate ( $B$ )

yields the approximate number of nodes that will do useful work. Unfortunately,  $r$  is difficult to ascertain without implementation and testing. An upper bound may be obtained by substituting  $m$  for  $r$ . By testing on a workfarm with a single farm node, as shown in Figure 4.8,  $m$  can be determined. The single workfarm node merely accepts request bundles and returns to the controller a simulated result bundle without doing any calculations. Thus an upper bound for the controller capacity is easily measured.

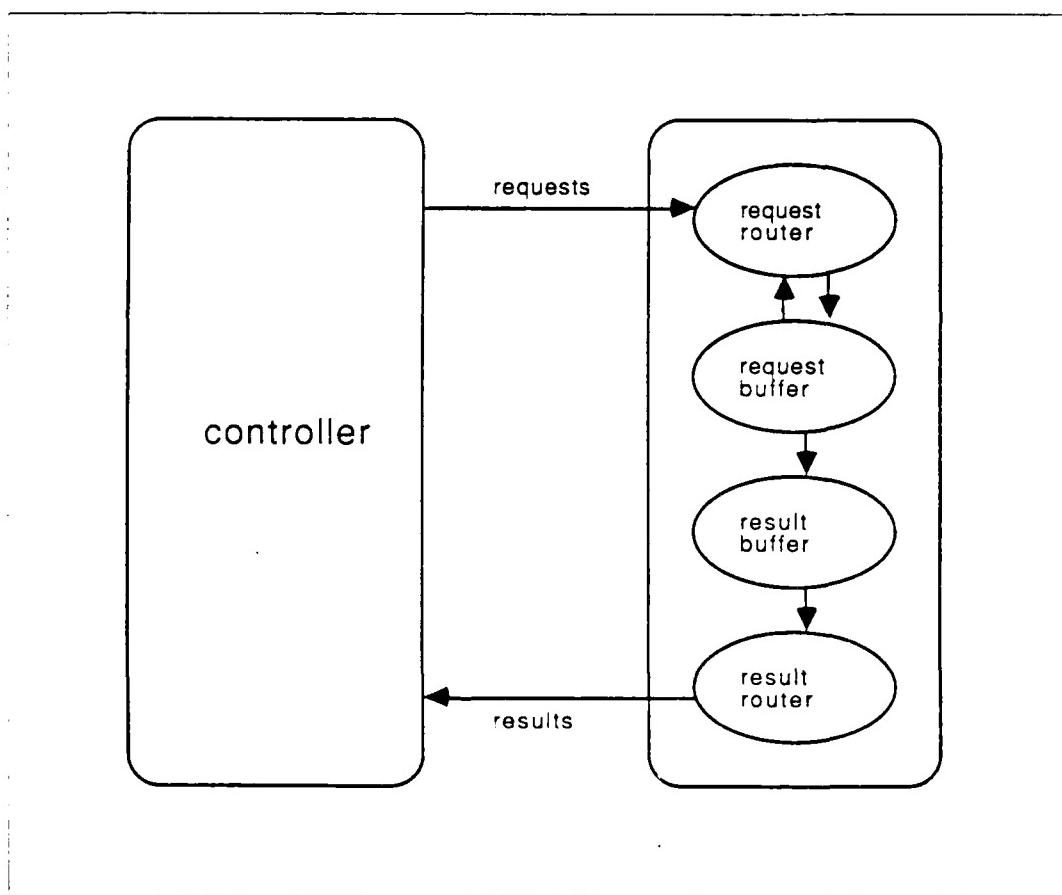
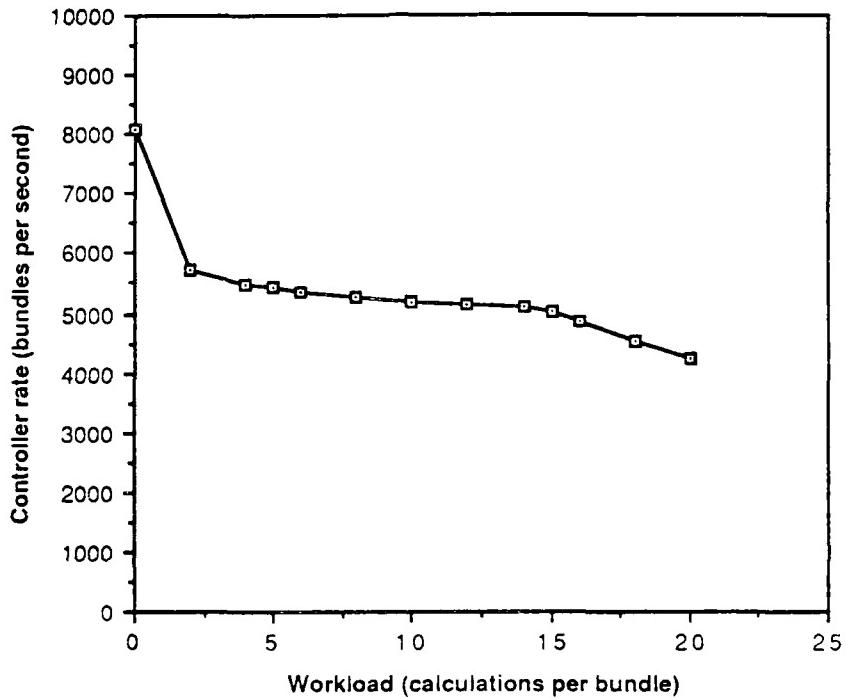


Figure 4.8  
Single Farm Node Test

Figure 4.9 shows the actual controller request bundle generation rate ( $r$ ) versus increasing workload for a farm consisting of 15 T414 nodes.

---



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Figure 4.9  
Controller Request Bundle Generation Rate

The initial rate versus a workload of zero is a high 8000 bundles per second. This zero workload rate, converted to 550 Kbytes per second, approaches the theoretical maximum unidirectional link rate of a T414, 750 Kbytes per second, and is in fact m. The zero workload rate will never match

the theoretical maximum rate because of the controller overhead. When a load is put on the farm, the actual rate drops off sharply to approximately 5700 bundles per second and then decreases gently at a nearly constant rate of approximately 100 rate units per workload unit. This rate holds until the farm begins to become calculation limited and the rate drops sharply again.

Since  $r$  is relatively constant during the communication limited portion of the graph, it can be used in the following rule of thumb equation for determining the maximum number of useful farm Transputers in a communication limited workfarm:

$$\text{Transputer limit} = \frac{r}{B}.$$

Again,  $m$  can be substituted for  $r$  in this equation to determine an upper bound on the number of Transputers a particular workload will utilize. Determining  $r$  accurately without testing the actual problem on a farm of multiple Transputers was a difficult problem. The only success in obtaining an approximate value of  $r$  was to test the actual problem on a farm of at least four Transputers. The resulting  $r$  value could then be used to project a Transputer limit for problems with larger workloads. The validity of this projection is a function of the accuracy of  $r$  and  $B$ .

Any time the number of Transputers in the farm is less than  $r + B$ , those Transputers are going to be fully utilized, each processing approximately  $N + n$  bundles.

## V. PREDICTIONS

### A. GENERAL

The research conducted in Chapter IV can be used to predict the performance of the workfarm in some cases. Two different problems are used in this chapter as examples: coordinate transformation and Mandelbrot set drawing. Actual performance results from these two problems were compared with the predictions.

### B. COORDINATE TRANSFORMATION PROBLEM

This coordinate transformation problem originated from research for a autonomous walking machine [Ri87]. The following is a brief description of the problem and its implementation on a workfarm. For in-depth coverage of the problem itself, the reader is referred to [Ri87].

An autonomous land vehicle, known as the Adaptive Suspension Vehicle, possesses an optical radar scanner which the vehicle uses to "see" the forward terrain. The scanner returns range measurements for each elevation and azimuth increment in its scan. A single scan consists of 128 azimuth increments for each of 128 elevation increments, a total of 16,384 iterations. The azimuth, elevation, and range are combined with six other inputs from the vehicle's inertial navigation system to develop a cartesian coordinate position of the particular scanned point. The elevation of every

point in the scan is kept in a terrain matrix data structure.

For the workfarm implementation, each packet represented one scan iteration and consisted of three bytes representing the scanner azimuth angle, the scanner elevation angle, and the resulting range. There were 16384 packets in one scan.

The vehicle's inertial navigation system (INS) supplied the vehicle attitude and position information, for a total of six inputs. The attitude information consisted of the vehicle's azimuth angle, pitch angle, and roll angle. The positional information consisted of the vehicle's x, y, and z transformation (distance) from the INS reference point. Because these six inputs remained constant for the entire scan, they could be passed to the farm and processed as much as possible during the initialization phase of the workfarm.

The radar scanner was easily implemented on a separate "scanner" process. Byte range values for a flat, zero elevation scan were calculated and then sequentially passed to the controller process through a channel. Although not implemented, the rate of outgoing range values could be easily controlled through use of the Transputer timer.

Each of the 16384 packets in a single scan were processed in the following way. Each byte in the packet was first hashed into a useful 32-bit floating point real number (REAL32). For example, the scanner azimuth range was -40 to +40 degrees. Since a byte can only represent the numbers 0

to 255, the scanner azimuth byte had to be converted into the correct data upon arrival in a farm node. Each bundle contained a byte tag and 128 packets.

For each packet the three new parameters were combined with the six parameters received during the initialization phase using a Denavit-Hartenberg (D-H) transformation to yield the x, y, and z coordinates of the particular spot being scanned [Ri87]. These three coordinates were themselves converted into bytes, loaded into the result bundle, and eventually passed back to the controller.

The problem was implemented on a standard workfarm as described in Chapters III and IV; that is, the controller process was placed on a T414-15 and eight farm nodes were placed on eight T800s. The scanner process was placed on a separate T414-15 and shared a single link with the controller process. The calculation process of a farm node is listed in Appendix C.

Testing on a single T800 Transputer yielded an approximate calculation rate (B) of 43.63 bundles per second. Total bundles for one scan (N) was 128.

The actual time for the workfarm to process a single scan (T) was 0.427 seconds, including loading the resultant 16384 altitude values into a terrair map matrix. The farm was controller limited, with 6.3 of the 8 Transputers being utilized.

The actual controller request bundle flow rate ( $r$ ) was 300 bundles per second. If this value of  $r$  could have been estimated correctly beforehand, the predicted Transputer limit for this problem would have been  $r$  divided by 8 or 6.9 Transputers. This is very close to the 6.3 Transputers that were actually utilized.

#### C. MANDELBROT SET

The drawing of the Mandelbrot Set is a problem that demonstrates the best qualities of the workfarm. It is a problem that is extremely computation intensive and where the amount of work each packet will entail is unknown.

For an in depth description of the Mandelbrot Set problem, the reader is directed to [Po86]; this chapter mainly discusses implementation and performance.

Essentially, the Mandelbrot set is generated by iterating a simple function on the points of the complex plane. The points that produce a cycle (the same value over and over again) fall in the set, whereas the points that diverge (give ever-growing values) lie outside it. When plotted on a computer screen in many colors (different colors for different rates of divergence), the points outside the set can produce pictures of great beauty. [Po86]

The problem is divided into independent work packets; each packet containing an integer tag and two other integers that represent a coordinate position on the complex plane. As stated before, the packet workload is variable; there is no way of knowing beforehand how much calculation each packet will require. Each packet really represents 16 coordinates because the farm node uses the single coordinate in

the packet as the starting point for 15 more consecutive horizontal coordinates. Each iteration can entail from one to 256 loops of approximately ten arithmetic operations each.

A factor in this particular problem is that the handler in the controller has to pass result bundles to the graphics routine on the B007 graphics board where the results are drawn. The controller flow rate ( $r$ ) is lowered because of this overhead.

The implementation of the Mandelbrot set onto the workfarm is somewhat different than in previous implementations. There is no benefit in bundling together packets to improve communication efficiency because of the variable packet workload. A request packet is already fairly large, 12 bytes, and a result packet is even larger, 32 bytes. Both request and result packets represent 16 coordinate points which can represent a massive amount of computation.

The generator and handler processes of the controller and the calculation process of the farm node are listed in Appendix D.

The problem was implemented on the same workfarm configuration as the coordinate transformation problem with the exception of the scanner.

The coordinate matrix was 512 by 512; thus there were 16384 packets ( $N$ ), each representing 16 horizontal coordinates as stated before.

When each coordinate only required one loop iteration, a solid dark gray screen was drawn in 1.5 seconds. The farm was controller limited as only 3.2 of the 8 Transputers were utilized. When each coordinate required 256 iterations, the workfarm required 81.5 seconds to draw a solid black screen. The farm, of course, was computation limited and all eight Transputers were utilized with only a slight variation in the number of packets processed by each.

Because the packet workload is variable, predictions are possible only when each coordinate represents the same amount of loop iterations; i.e., the screen is solid black (256 iterations per coordinate) or solid dark gray (one iteration per coordinate).

Testing on a single T800 Transputer yielded an approximate calculation rate ( $B$ ) of 39 packets per second. Using this value in the calculation limited equation to predict the actual time to draw a solid black screen on a farm of eight T800 Transputers yielded 52.5 seconds. As noted previously, however, the actual time was 81.5 seconds. This discrepancy arose because the controller was limiting the farm although the problem was still calculation limited. The controller limited the farm because the controller's handler had to send every results packet to the graphics Transputer for drawing. This caused the controller to wait because the graphics process would not accept another packet

until the previous one had been completed (drawn). This waiting translated into significant overhead.

The actual problem was again tested, this time without the controller handler having to pass results to the graphics Transputer (no picture was drawn); the controller handler merely accepted results from the farm. The actual time in this case was approximately 53 seconds, very close to the original prediction.

Clearly, the equations do not work if the controller has to do work on the results after reception. In this case, for the equations to remain applicable, the controller handler needs to relay work to a buffer Transputer between the controller and the graphics Transputer (for example). Or, if much work of a different type is needed, the results could be passed to another, separate farm.

## VI. CONCLUSIONS AND RECOMMENDATIONS

### A. CONCLUSIONS

This thesis deals primarily with the work distribution algorithm known as *workfarm*. Although limited to problems divisible into independent work packets, it is a simple yet extremely effective way of processing in parallel and achieving near linear performance speedups. Processing rapid streams of data from a weapon system sensor would seem to fall into the *workfarm* category of problems. The coordinate transformation example demonstrates that the *workfarm* is well suited for a radar problem.

### B. RECOMMENDATIONS

Although the equations for *workfarm* performance have been developed in this thesis, research on how to accurately estimate the controller request bundle flow rate for a farm of a given number of Transputers and given workload needs to be done to predict the limit at which a farm becomes controller limited. For the same reason, research is needed to accurately estimate the degradation factor for each node in the farm.

Both the pipeline and *workfarm* are good for specific types of problems; however, much work remains in developing and evaluating new work distribution algorithms for other

kinds of problems. Specifically, [HwCh87] appears promising as a source for new work distribution algorithms.

Much work remains, too, in development and evaluation of new network physical topologies. For example, in a workfarm, a simple binary tree farm topology would allow a controller to supply the farm with a far greater rate of request bundles than it could to a linear array farm. Other topologies, such as hypernet [HwGh87], would be extremely interesting to implement. Currently there are too few Transputers in the lab to significantly explore these different topologies; perhaps, more topology research can be done when greater numbers of Transputers are available. The relative ease to configure multi-Transputer networks by virtue of the OCCAM programming language makes widespread research in network topology practical for the first time.

An ADA compiler will be available for the Transputer family soon; since ADA is the Department of Defense standard programming language, research on the implementation of Ada on Transputers should begin as soon as the compiler arrives.

The ultimate goal of an ongoing series of Transputer theses at the U.S. Naval Postgraduate School, of which this thesis is part, is to develop an alternative computer architecture for the U.S. Navy Aegis Combat System. The expertise base represented by this series of theses has reached the point where the next step should be the simulation of the AN/SPY-1A 3D Phased Array Radar Controller, the main

component of the Aegis Combat System. It seems likely that the workfarm would have some utility in such a simulation.

One fact stands out from working with Transputers: the Transputer system is revolutionary. Its performance jump over anything short of a supercomputer is orders of magnitude. True parallel processing is implemented easily with a high level programming language, employing the best elements of software engineering. The Transputer system seems especially useful for the military, considering the Transputers suitability for embedded control applications and parallel processing networks.

## APPENDIX A

### BINARY TREE WORKFARM SOURCE CODE

The only difference between the binary tree and the linear array workfarms occurs in the request and result routers of the farm node. To keep the program compact, two separate versions of the farm node were developed, a fork node and a leaf node. That is all that is listed in this appendix. The complete algorithm for a linear array workfarm is in Appendix B.

```
-----  
PROC fork(CHAN OF ANY    requests.in, requests.out.left,  
          requests.out.right,  
          results.in.left, results.in.right,  
          results.out,  
          VAL INT      proc.id)  
-----  
CHAN OF ANY    from.result.router, signal:  
CHAN OF ANY    to.buffer, to.calculation:  
CHAN OF ANY    from.buffer, from.calculation:  
  
PRI PAR  
  PAR  
    VAL left IS FALSE:  
    VAL right IS TRUE:  
    ... communication  
    ... calculation  
:  
:
```

```

----- fork request router -----
--- declarations
[bundle.size]BYTE bundle:
INT    tag RETYPES [bundle FROM 0 FOR 4]:
BOOL   d.buffer.empty, switch:
INT    num.left, num.right:

SEQ
  --- initialization
  d.buffer.empty := TRUE
  IF
    proc.id = 0
    SEQ
      num.left := 6
      num.right := 6
    proc.id > 0
    SEQ
      num.left := 2
      num.right := 2

WHILE TRUE
  PRI ALT
  ALT
    signal ? d.buffer.empty
    SKIP
    from.result.router ? switch
    IF
      switch = left
      num.left := num.left + 1
      switch = right
      num.right := num.right + 1
  requests.in ? bundle
  IF
    tag = data
    IF
      d.buffer.empty
      SEQ
        d.buffer.empty := FALSE
        to.buffer ! bundle
    else
      IF
        num.left >= num.right
        SEQ
          num.left := num.left - 1
          requests.out.left ! bundle
    else
      SEQ
        num.right := num.right - 1
        requests.out.right ! bundle

```

```

tag = setup
PAR
    requests.out.left ! bundle
    requests.out.right ! bundle
    to.buffer ! bundle

tag = report
PAR
    requests.out.left ! bundle
    requests.out.right ! bundle
    to.buffer ! bundle

-----
fork result router
-----
[bundle.size]BYTE bundle:
WHILE TRUE
PRI ALT
from.buffer ? bundle
    results.out ! bundle
results.in.left ? bundle
PAR
    from.result.router ! left
    results.out ! bundle
results.in.right ? bundle
PAR
    from.result.router ! right
    results.out ! bundle

```

```
-----  
PROC leaf(CHAN OF ANY      requests.in, results.out,  
          VAL INT        proc.id)  
-----
```

```
CHAN OF ANY  signal:  
CHAN OF ANY  to.buffer, to.calculation:  
CHAN OF ANY  from.buffer, from.calculation:  
PRI PAR  
PAR  
    ... communication  
    ... calculation  
:  
-----
```

```
leaf request router  
-----
```

```
-- declarations
```

```
[bundle.size]BYTE bundle:  
INT      tag RETYPES  [bundle FROM 0 FOR 4]:  
BOOL     d.buffer.empty:
```

```
SEQ
```

```
    d.buffer.empty := TRUE  
    WHILE TRUE
```

```
        PRI ALT
```

```
            signal ? d.buffer.empty
```

```
                SKIP
```

```
            requests.in ? bundle
```

```
                IF
```

```
                    tag = data
```

```
                    IF
```

```
                        d.buffer.empty
```

```
                        SEQ
```

```
                            d.buffer.empty := FALSE
```

```
                            to.buffer ! bundle
```

```
                else
```

```
                    SKIP
```

```
                tag = setup
```

```
                to.buffer ! bundle
```

```
                tag = report
```

```
                to.buffer ! bundle
```

```
leaf result router  
-----
```

```
[bundle.size]BYTE bundle:
```

```
WHILE TRUE
```

```
    SEQ
```

```
        from.buffer ? bundle
```

```
        results.out ! bundle
```

APPENDIX B  
GENERIC WORKFARM SOURCE CODE

```
--- global variable file
VAL MAXnumT8           IS     8:
VAL total.bundles       IS     625:
VAL total.packets        IS    10000:

VAL packets.per.bundle IS   total.packets/total.bundles:
VAL bundle.size.int    IS   packets.per.bundle + 1:

VAL packet.size.int    IS     1:
VAL base.calc           IS     10:
VAL calc.loops          IS     10:
VAL bundle.size         IS   bundle.size.int TIMES 4:
VAL packet.size         IS   packet.size.int TIMES 4:

VAL farmSIZE            IS   MAXnumT8:
VAL workSIZE            IS   (farmSIZE TIMES 2) - 1:
VAL data                IS     1:
VAL setup               IS     2:
VAL report              IS     3:
VAL else                IS   TRUE:

-----
PROC root(CHAN OF ANY to.graph, from.graph, requests,
          results)
-----
--- internal channels
CHAN OF ANY to.handler, from.handler,
          to.router, from.router,
          trigger:

PAR
  generator(to.router, to.handler, from.handler)
  work.router(to.router, trigger, requests)
  results.router(from.router, trigger, results)
  handler(from.router, to.handler, from.handler, to.graph,
          from.graph)
:
```

```
-----  
PROC node(CHAN OF ANY      requests.in, requests.out,  
          VAL INT           results.in, results.out,  
                           proc.id)  
-----  
    --- internal channel declarations  
    CHAN OF ANY      to.buffer, to.calculation:  
    CHAN OF ANY      from.calculation, from.buffer:  
    CHAN OF BOOL     signal:  
  
    PRI PAR  
    PAR  
        ... request router  
        ... request buffer  
        ... result buffer  
        ... result router  
        ... calculation  
:  
:
```

```

-----  

PROC generator(CHAN OF ANY to.router, to.handler,  

               from.handler)  

-----  

    --- declarations  

    [bundle.size]BYTE      bundle:  

    INT      tag           RETYPES  [bundle FROM 0 FOR 4]:  

    []INT     setup.array   RETYPES  [bundle FROM 4 FOR 8]:  

    INT      any:  

    SEQ calcs.per.packet = 1 FOR calc.loops  

    SEQ  

        --- start clock  

        to.handler ! calcs.per.packet  

        --- initialize nodes  

        tag := setup  

        to.router ! bundle  

        --- generate and send packets  

        tag := data  

        setup.array[0] := base.calc TIMES calcs.per.packet  

        SEQ j = 0 FOR total.bundles  

            to.router ! bundle  

        --- wait till all results have been received and  

        graphed  

        from.handler ? any  

        --- request report  

        tag := report  

        to.router ! bundle  

:  


```

```

-----  

PROC results.router(CHAN OF ANY from.router, trigger,  

                     results)  

-----  


```

```

    --- declarations  

    [bundle.size]BYTE  bundle :  

    VAL packet.done    IS  TRUE :  

    WHILE TRUE  

    SEQ  

        results ? bundle  

        PAR  

            trigger ! packet.done  

            from.router ! bundle  

:  


```

```

-----  

PROC work.router(CHAN OF ANY to.router, trigger, requests)  

-----  

    --- declarations  

    [bundle.size]BYTE bundle:  

    INT tag RETYPES [bundle FROM 0 FOR 4]:  

    BOOL packet.done, reporting:  

    INT workCOUNT:  

    SEQ  

        --- initialization  

        workCOUNT := 0  

        reporting := FALSE  

        WHILE TRUE  

            PRI ALT  

                trigger ? packet.done  

                IF  

                    NOT reporting  

                    workCOUNT := workCOUNT - 1  

                else  

                    SKIP  

                (workCOUNT <= workSIZE) & to.router ? bundle  

                IF  

                    tag = data  

                    SEQ  

                        requests ! bundle  

                        workCOUNT := workCOUNT + 1  

                    tag = setup  

                    SEQ  

                        reporting := FALSE  

                        requests ! bundle  

                    tag = report  

                    SEQ  

                        reporting := TRUE  

                        requests ! bundle  

:

```

```

-----  

PROC handler(CHAN OF ANY from.router, to.handler,  

            from.handler, screen, keyboard)  

-----  

    --- declarations  

    [bundle.size]BYTE      bundle:  

    [ ]INT report.array   RETYPES  [bundle FROM 0 FOR 8]:  

    INT node.id           IS        report.array[0]:  

    INT num.node.bundles IS        report.array[1]:  

    VAL go                IS        1:  

    TIMER clock:  

    INT start.time, stop.time:  

    INT calcs.per.packet:  

    SEQ  

        WHILE TRUE  

        SEQ  

            --- start clock on controls command  

            to.handler ? calcs.per.packet  

            clock ? start.time  

            --- receive data packets  

            SEQ i = 0 FOR total.bundles  

                from.router ? bundle  

            --- stop the timer  

            clock ? stop.time  

            --- let controller know all done graphing  

            from.handler ! go  

            --- make terminal report  

            write.int(screen,(stop.time-start.time) TIMES 64,9)  

            write.int(screen,(calcs.per.packet TIMES  

                                base.calc), 4)  

            SEQ i = 0 FOR farmSIZE  

            SEQ  

                from.router ? bundle  

                write.int(screen, num.node.bundles, 4)  

                newline(screen)
:

```

```

----- request router -----
--- declarations
[bundle.size]BYTE bundle:
INT tag RETYPES [bundle FROM 0 FOR 4]:
BOOL d.buffer.empty :

SEQ
d.buffer.empty := TRUE
WHILE TRUE
PRI ALT
signal ? d.buffer.empty
SKIP
requests.in ? bundle
IF
tag = data
IF
d.buffer.empty
SEQ
d.buffer.empty := FALSE
to.buffer ! bundle
else
requests.out ! bundle

tag = setup
IF
proc.id < (MAXnumT8-1)
PAR
requests.out ! bundle
to.buffer ! bundle

else --- last node
to.buffer ! bundle

tag = report
IF
proc.id < (MAXnumT8-1)
PAR
requests.out ! bundle
to.buffer ! bundle
else
to.buffer ! bundle

```

```
-----  
                                request buffer  
-----  
--- declarations  
[bundle.size]BYTE bundle:  
INT tag RETYPES [bundle FROM C FOR 4]:  
VAL buffer.empty IS TRUE :  
  
WHILE TRUE  
SEQ  
    to.buffer ? bundle  
    IF  
        tag = data  
        SEQ  
            to.calculation ! bundle  
            signal ! buffer.empty  
  
        tag = setup  
        to.calculation ! bundle  
        tag = report  
        to.calculation ! bundle
```

```
-----  
                                result buffer  
-----  
[bundle.size]BYTE bundle:  
WHILE TRUE  
SEQ  
    from.calculation ? bundle  
    from.buffer ! bundle
```

```
-----  
                                result router  
-----  
[bundle.size]BYTE bundle:  
WHILE TRUE  
PRI ALT  
    from.buffer ? bundle  
    results.out ! bundle  
    results.in ? bundle  
    .results.out ! bundle
```

```

----- calculation -----
----- declarations -----
[bundle.size]BYTE      bundle.in, bundle.out:
[]INT setup.array      RETYPES [bundle.in FROM 4 FOR 8]:
[]INT report.array     RETYPES [bundle.out FROM 0 FOR 8]:
[packet.size]BYTE      work.array:
INT tag RETYPES        [bundle.in FROM 0 FOR 4]:
INT calcs.per.packet IS setup.array[0]:
INT num.node.bundles:
REAL32 x:

SEQ
  WHILE TRUE
    SEQ
      to.calculation ? bundle.in
      IF
        tag = data
        SEQ
          SEQ i = 1 FOR packets.per.bundle
          SEQ
            [work.array FROM 0 FOR 4] := [bundle.in FROM
              (i TIMES 4) FOR 4]
            SEQ j = 0 FOR calcs.per.packet
              x := x*x
              SEQ j = 0 FOR packet.size
                bundle.out[j] := 2(BYTE)

            from.calculation ! bundle.out
            num.node.bundles := num.node.bundles + 1

        tag = setup
        SEQ
          num.node.bundles := 0
          x := 0.9999(REAL32)

        tag = report
        SEQ
          report.array[0] := proc.id
          report.array[1] := num.node.bundles
          from.calculation ! bundle.out

```

## APPENDIX C

### COORDINATE TRANSFORMATION PROBLEM SOURCE CODE

Only those portions of code different from that of the generic workfarm are included in this Appendix.

```
--- global variable file
VAL total.bundles      IS    128:
VAL total.packets      IS   16384:
VAL packets.per.bundle IS total.packets/total.bundles:
VAL bundle.size        IS    385:

-----
PROC generator(CHAN OF ANY to.router, to.handler,
               from.handler, from.scanner)
-----
--- declarations
[bundle.size]BYTE  bundle:
[ ]REAL32 setup.array RETYPES [bundle FROM 4 FOR 24]:
BYTE  tag      IS bundle[0]:
REAL32 ASV.pitch IS setup.array[0]:
REAL32 ASV.az    IS setup.array[1]:
REAL32 ASV.roll   IS setup.array[2]:
REAL32 ASV.x     IS setup.array[3]:
REAL32 ASV.y     IS setup.array[4]:
REAL32 ASV.z     IS setup.array[5]:
INT   index, any:

SEQ
--- start clock
to.handler ! 1

--- initialize nodes
tag := setup
ASV.pitch   := 0.0(REAL32) ---asv.pitch
ASV.az      := 0.0(REAL32) ---asv.az
ASV.roll    := 0.0(REAL32) ---asv.roll
ASV.x       := 0.0(REAL32) ---asv.x
ASV.y       := 64.0(REAL32) ---asv.y
ASV.z       := -8.0(REAL32) ---asv.z
to.router ! bundle
```

```

--- generate and send packets
tag := data
SEQ i = 0 FOR 128
  SEQ
    SEQ j = 0 FOR 128
      SEQ
        index := j TIMES 3
        bundle[index+1] := BYTE i
        bundle[index+2] := BYTE j
        from.scanner ? bundle[index+3]
      to.router ! bundle

--- request report
from.handler ? any
tag := report
to.router ! bundle
:

-----  

PROC handler(CHAN OF ANY from.router, to.handler,
             from.handler, to.graph, from.graph)
-----  

--- declarations
[128][128]INT terrain.map:
[bundle.size]BYTE bundle:
[]INT report.array RETYPES [bundle FROM 0 FOR 8]:
INT node.id IS report.array[0]:
INT node.bundles IS report.array[1]:
VAL ready IS 1:
INT start.time, stop.time :
INT total.bundles:
TIMER clock:
INT x.int, y.int, z.int:
INT any, index:

SEQ
--- init
SEQ i = 0 FOR 128
  SEQ j = 0 FOR 128
    terrain.map[i][j] := 0

WHILE TRUE
  SEQ
    --- start clock on controls command
    to.handler ? any
    clock ? start.time

```

```

---- receive data packets
SEQ i = 0 FOR 128
SEQ
  from.router ? bundle
  SEQ j = 0 FOR 128
  SEQ
    index := j TIMES 3
    x.int := INT bundle[index]
    y.int := INT bundle[index+1]
    z.int := (INT bundle[index+2]) - 128
    terrain.map[y.int][x.int] := z.int

--- stop the timer
clock ? stop.time

--- let controller know all done graphing
from.handler ! ready

--- make terminal report
newline(to.graph)
newline(to.graph)
write.int(to.graph,(stop.time-start.time)*64,10)
newline(to.graph)
total.bundles := 0
SEQ i = 0 FOR farmSIZE
SEQ
  from.router ? bundle
  write.int(to.graph, node.id, 3)
  write.int(to.graph, node.bundles, 10)
  total.bundles := total.bundles + node.bundles
  newline(to.graph)
newline(to.graph)
write.int(to.graph, total.bundles, 13)

--- display wire terrain graph on SONY
[128]INT altitude.array:
VAL XMID IS 256:
VAL YBASE IS 450:
VAL scalefactor IS 200000/256:
INT reply, horiz, vert, x.old, y.old, x.new, y.new:
INT horizl, vertl:

```

```

SEQ
--- initialization
SEQ i = 0 FOR 128
    altitude.array[i] := 512
vert := 0
to.graph ! c.select.bg.colour;24
from.graph ? reply
to.graph ! c.select_fg.colour;2
from.graph ? reply
to.graph ! c.init.crt
from.graph ? reply
to.graph ! c.select.screen;0
from.graph ? reply
to.graph ! c.clear.screen;0
from.graph ? reply
to.graph ! c.display.screen;0
from.graph ? reply
to.graph ! c.move;256;450
from.graph ? reply

SEQ i = 0 FOR 128
SEQ
    horiz := 2
    horizl := (horiz * scalefactor)/1000
    vertl := (vert * scalefactor)/1000
    x.old := XMID - vert
    y.old := YBASE - (vertl + terrain.map[i][0])

--- process row
SEQ j = 1 FOR 127
SEQ
    x.new := (XMID + horiz) - vert
    y.new := YBASE - (horizl + (vertl +
        terrain.map[i][j]))
--- drawline
IF
    y.new < altitude.array[j]
    SEQ
        to.graph ! c.draw.line; x.old;
            y.old; x.new; y.new
        from.graph ? reply
        altitude.array[j] := y.new
    else
        SKIP
    x.old := x.new
    y.old := y.new
    horiz := horiz + 2
    horizl := (horiz * scalefactor)/1000
    vert := vert + 2
:

```

```

----- Calculation -----
-----  

--- bundle declarations  

[bundle.size]BYTE      bundle.in:  

[bundle.size]BYTE      bundle.out:  

[]REAL32 setup.array RETYPES [bundle.in FROM 4 FOR 24]:  

[]INT    report.array RETYPES [bundle.out FROM 0 FOR 8]:  

BYTE      tag           IS      bundle.in[0]:  

INT      node.bundles:  

--- computation variables  

BYTE      x.byte, y.byte, z.byte:  

INT      x.int, y.int, z.int:  

REAL32   x.real, y.real, z.real:  

REAL32   a,b,c,e,f,g,i,j,k:  

REAL32   c4c5, s4c5, d9s8, four, eight, twelve:  

REAL32   c4,c5,c6,c7,c8,s4,s5,s6,s7,s8,a7,d9:  

REAL32   scanner.az, scanner.pitch, target.range:  

REAL32   ASV.x, ASV.y, ASV.z, ASV.az, ASV.pitch, ASV.roll:  

REAL32   temp1, temp2, temp3, temp4:  

BYTE      raw.scanner.pitch, raw.scanner.az, raw.target.range:  

--- constants  

VAL Pi      IS 3.1416(REAL32):  

VAL PiBy2   IS Pi/2.0(REAL32):  

VAL factor IS Pi/180.0(REAL32):  

INT      index:  

SEQ
  WHILE TRUE
  SEQ
    to.calculation ? bundle.in
    IF
      tag = data
      SEQ
        SEQ z = 0 FOR 128
        SEQ
          index := z TIMES 3
          --- process raw data packet:
          --- pitch into degrees from -15 to -75
          --- convert az into degrees from -40 to +40
          --- convert range into feet from 0 to 32

          templ := REAL32 ROUND
                  (INT bundle.in[index+1])
          temp2 := 15.0(REAL32)
          temp3 := 1.47244(REAL32) * templ
          scanner.pitch := templ - (temp2 + temp3)

```

```

temp4 := REAL32 ROUND
        (INT bundle.in[index+2])
scanner.az := (temp4 * 0.6299(REAL32)) -
        40.0(REAL32)

target.range := (REAL32 ROUND
        (INT bundle.in[index+3]))/8.0(REAL32)

--- do sines and cosines
scanner.pitch := (factor * scanner.pitch) -
        PiBy2
scanner.az := (factor * scanner.az) - PiBy2
COSP(c7, scanner.pitch)
COSP(c8, scanner.az)
SINP(s7, scanner.pitch)
SINP(s8, scanner.az)

--- assign variables
d9s8 := s8*target.range
four := (d9s8 * c7) + (a7 * c7)
eight := (d9s8 * s7) + (a7 * s7)
twelve := c8*target.range

--- calculate 3 points of the 4x4 matrix
x.real := ASV.x + ((a * four) + ((b * eight)
        + (c * twelve)))
y.real := ASV.y + ((e * four) + ((f * eight)
        + (g * twelve)))
z.real := ASV.z + ((i * four) + ((j * eight)
        + (k * twelve)))

--- convert results into bytes
bundle.out[index] := BYTE (INT ROUND x.real)
bundle.out[index+1] := BYTE (INT ROUND
        y.real)
bundle.out[index+2] := BYTE ((INT ROUND
        z.real) + 128)
from.calculation ! bundle.out
node.bundles := node.bundles + 1

tag = setup
SEQ
    node.bundles := 0
    ASV.pitch := setup.array[0]
    ASV.az := setup.array[1]
    ASV.roll := setup.array[2]
    ASV.x := setup.array[3]
    ASV.y := setup.array[4]
    ASV.z := setup.array[5]

```

```

--- convert degrees into radians
ASV.pitch := factor * ASV.pitch
ASV.az     := factor * ASV.az
ASV.roll   := factor * ASV.roll

--- do sines and cosines
SINP(s4, (ASV.az + Pi))
SINP(s5, (ASV.pitch - PiBy2))
SINP(s6, (ASV.roll + Pi))
COSP(c4, (ASV.az + Pi))
COSP(c5, (ASV.pitch - PiBy2))
COSP(c6, (ASV.roll + Pi))

--- assign variables
c4c5 := c4*c5
s4c5 := s4*c5

a := (c4c5*c6)+(s4*s6)
b := c4*s5
c := (c4c5*s6)-(s4*c6)

e := (s4c5*c6)-(c4*s6)
f := s4*s5
g := (s4c5*s6)+(c4*c6)

i := s5*c6
j := -c5
k := s5*s6

a7 := -0.5(REAL32)

tag = report
SEQ
    report.array[0] := proc.id
    report.array[1] := node.bundles
    from.calculation ! bundle.out

```

```

-----  

PROC scanner (CHAN OF ANY from.scanner)
-----  

    --- declarations  

    [128][128]BYTE      range:  

    VAL                  Pi           IS 3.1416(REAL32):  

    VAL                  factor        IS Pi/180.0(REAL32):  

    REAL32                angle.deg, angle.rad, cosangle, deg.inc:  

    BYTE                 range.byte:  

    SEQ  

        --- initialize array of range values  

        angle.deg := 75.0(REAL32)  

        angle.rad := factor * angle.deg  

        COSP(cosangle, angle.rad)  

        range.byte := BYTE (INT ROUND (64.0(REAL32)/cosangle))  

        SEQ i = 0 FOR 128  

            SEQ  

                SEQ j = 0 FOR 128  

                    range[i][j] := range.byte  

                    angle.deg := angle.deg - 0.46875(REAL32)  

                    angle.rad := factor * angle.deg  

                    COSP(cosangle, angle.rad)  

                    range.byte := BYTE (INT ROUND  

                        (64.0(REAL32)/cosangle))  

            --- pump out range BYTES  

            SEQ i = 0 FOR 128  

                SEQ j = 0 FOR 128  

                    from.scanner ! range[i][j]
:

```

## APPENDIX D

### MANDELBROT SET PROBLEM SOURCE CODE

```
--- Mandelbrot global constants
VAL MAXnumT8      IS 8:
VAL packetSIZE    IS 16:
VAL else          IS TRUE:
VAL rSIZE         IS 512:
VAL iSIZE         IS 512:
VAL rSTEPS        IS rSIZE/packetSIZE:
VAL packetCOUNT   IS rSTEPS * iSIZE :
VAL countLIMIT    IS 255:

VAL farmSIZE      IS MAXnumT8:
VAL workSIZE      IS (farmSIZE * 2) - 1 :

VAL data          IS 1:
VAL setup         IS 2:
VAL report        IS 3:

-----
PROC root(CHAN OF ANY to.graph, from.graph,
          requests, results)
-----
-- internal channels
CHAN OF ANY      to.router, from.router:
CHAN OF ANY      to.handler, from.handler:
CHAN OF ANY      trigger:

VAL zoom.in       IS 0:
VAL zoom.out      IS 1:
VAL rSIZE.real    IS (REAL64 ROUND rSIZE):
VAL iSIZE.real    IS (REAL64 ROUND iSIZE):

PAR
  generator(to.router, to.handler, from.handler)
  work.router(to.router, trigger, requests)
  results.router(from.router, trigger, results)
  handler(from.router, to.handler, from.handler, to.graph,
          from.graph)
:
```

```

-----  

PROC generator(CHAN OF ANY to.router, to.handler,  

               from.handler)  

-----  

-- data variables  

[12]BYTE data.array:  

INT tag RETYPES [data.array FROM 0 FOR 4]:  

[]INT START RETYPES [data.array FROM 4 FOR 8]:  

INT rSTART IS START[0]:  

INT iSTART IS START[1]:  

REAL64 setup.value RETYPES [data.array FROM 4 FOR 8]:  

REAL64      rMIN, rMAX, iMIN, iMAX :  

REAL64      rMIN.temp, rMAX.temp, iMIN.temp, iMAX.temp :  

REAL64      ul.x.real,ul.y.real,lr.x.real,lr.y.real:  

REAL64      rMID, iMID:  

INT        mode :  

INT        any, ul.x, ul.y, lr.x, lr.y :  

SEQ  

  rMIN := -2.0(REAL64)  

  rMAX := 0.5(REAL64)  

  iMIN := 1.25(REAL64)  

  iMAX := -1.25(REAL64)  

  WHILE TRUE  

    SEQ  

      --- initialize nodes  

      tag := setup  

      setup.value := rMIN  

      to.router ! data.array  

      setup.value := rMAX  

      to.router ! data.array  

      setup.value := iMIN  

      to.router ! data.array  

      setup.value := iMAX  

      to.router ! data.array  

      to.handler ! 1  

      --- send packets  

      tag := data  

      SEQ i = 0 FOR iSIZE  

        SEQ  

          iSTART := i  

          SEQ j = 0 FOR rSTEPS  

            SEQ  

              rSTART := j * packetSIZE  

              to.router ! data.array  

      --- report  

      from.handler ? any  

      tag := report  

      to.router ! data.array

```

```

--- get new plot coordinates
from.handler ? mode; ul.x; ul.y; lr.x; lr.y
INT32TOREAL64(ul.x.real,ul.x)
INT32TOREAL64(ul.y.real,ul.y)
INT32TOREAL64(lr.x.real,lr.x)
INT32TOREAL64(lr.y.real,lr.y)
ul.x.real := REAL64 ROUND ul.x
ul.y.real := REAL64 ROUND ul.y
lr.x.real := REAL64 ROUND lr.x
lr.y.real := REAL64 ROUND lr.y
IF
    mode = zoom.in
    SEQ
        rMIN.temp := (((rMAX-rMIN)*ul.x.real)
                      /rSIZE.real)+rMIN
        rMAX.temp := (((rMAX-rMIN)*lr.x.real)
                      /rSIZE.real)+rMIN
        iMIN.temp := (((iMIN-iMAX)*lr.y.real)
                      /iSIZE.real)+iMAX
        iMAX.temp := (((iMIN-iMAX)*ul.y.real)
                      /iSIZE.real)+iMAX
        rMIN := rMIN.temp
        rMAX := rMAX.temp
        iMIN := iMIN.temp
        iMAX := iMAX.temp
    mode = zoom.out
    REAL64 scale.factor:
    SEQ
        scale.factor := rSIZE.real/
                        (lr.x.real-ul.x.real)
        rMID := (rMAX + rMIN)/(2.0(REAL64))
        iMID := (iMAX + iMIN)/(2.0(REAL64))
        rMIN := rMID - (scale.factor*(rMID-rMIN))
        rMAX := rMID + (scale.factor*(rMAX-rMID))
        iMIN := iMID - (scale.factor*(iMID-iMIN))
        iMAX := iMID + (scale.factor*(iMAX-iMID))
:

```

```

-----  

PROC handler(CHAN OF ANY from.router, to.handler,  

            from.handler, to.graph, from.graph)  

-----  

    --- declarations  

    [16 + packetSIZE]BYTE graph.array :  

    INT v.c.man RETYPES [graph.array FROM 0 FOR 4]:  

    INT v.pSIZE RETYPES [graph.array FROM 4 FOR 4]:  

    [ ]BYTE result.array IS [graph.array FROM 8 FOR  

                            (8+packetSIZE)]:  

    INT node.packets RETYPES [result.array FROM 0 FOR 4]:  

    INT node.loops RETYPES [result.array FROM 4 FOR 4]:  

    BYTE node.id IS result.array[8]:  

    INT range, reply:  

    INT n.x, n.y, m.x, m.y, l.x,l.y, buttons:  

    INT delta.x, delta.y:  

    BOOL m.l, m.m, m.r, select.ok, done.select:  

    INT start.time, stop.time, recirc:  

    INT total.loops, total.packets:  

    TIMER clock:  

    INT any:  

    SEQ  

        --- initialization  

        v.c.man := c.mandelbrot  

        v.pSIZE := packetSIZE  

    WHILE TRUE  

        SEQ  

            --- init graphics display  

            to.graph ! c.hide.cursor  

            from.graph ? reply  

            to.graph ! c.init.crt  

            from.graph ? reply  

            to.graph ! c.select.screen ; 0  

            from.graph ? reply  

            to.graph ! c.clear.screen ; 0  

            from.graph ? reply  

            to.graph ! c.display.screen; 0  

            from.graph ? reply  

            to.graph ! c.select.colour.table; 1  

            from.graph ? reply  

            to.graph ! c.set.colour; countLIMIT; 0; 0; 0  

            from.graph ? reply  

            --- start clock  

            to.handler ? any  

            clock ? start.time

```

```

--- receive packets
SEQ i = 0 FOR packetCOUNT
  SEQ
    from.router ? result.array
    to.graph ! graph.array

--- stop clock
clock ? stop.time

--- let controller know all done
from.handler ! 1

--- make terminal report
newline(to.graph)
newline(to.graph)
write.int(to.graph,(stop.time-start.time)*64,10)
newline(to.graph)
total.loops := 0
total.packets := 0
SEQ i = 0 FOR farmSIZE
  BYTE char:
  SEQ
    from.router ? result.array
    write.int(to.graph,(INT node.id),3)
    write.int(to.graph,node.packets,10)
    write.int(to.graph,node.loops,10)
    total.loops := total.loops + node.loops
    total.packets := total.packets + node.packets
    newline(to.graph)
  newline(to.graph)
  write.int(to.graph, total.packets, 13)
  write.int(to.graph, total.loops, 10)
  newline(to.graph)
  write.int(to.graph,
            (512*(512/packetSIZE))-total.packets,13)
  write.int(to.graph,total.loops/total.packets,10)
  newline(to.graph)
  newline(to.graph)

--- get the new coordinates for calculation
--- set-up for rectangle
to.graph ! c.copy.screen; 0
from.graph ? reply
to.graph ! c.select.fg.colour; 15
from.graph ? reply

--- get the current mouse stats
to.graph ! c.show.cursor
from.graph ? reply
done.select := FALSE
select.ok := FALSE

```

```

WHILE NOT done.select
SEQ
--- wait for any mouse button to be pressed
to.graph ! c.get.mouse
from.graph ? n.x;n.y;m.l;m.m;m.r
WHILE (NOT m.m) AND ((NOT m.l) AND (NOT m.r))
SEQ
to.graph ! c.get.mouse
from.graph ? n.x;n.y;m.l;m.m;m.r

IF
m.m
BOOL new.select:
SEQ
m.x := n.x
m.y := n.y
l.x := m.x
l.y := m.y
new.select := TRUE

--- process mouse input until middle mouse
--- is released
WHILE m.m
SEQ
to.graph ! c.get.mouse
from.graph ? n.x;n.y;m.l;m.m;m.r
IF
((n.x <> l.x) OR (n.y <> l.y)) OR
new.select
SEQ
new.select := FALSE
to.graph ! c.hide.cursor
from.graph ? reply
to.graph ! c.copy.screen; 1
from.graph ? reply

--- set new corner coordinates
delta.x := n.x - m.x
delta.y := n.y - m.y
IF
delta.x > 0
IF
delta.y > 0
IF
delta.x > delta.y
delta.x := delta.y
TRUE
delta.y := delta.x

```

```

        TRUE
        IF
            delta.x > (-delta.y)
            delta.x := -delta.y
        TRUE
            delta.y := -delta.x

        TRUE
        IF
            delta.y > 0
            IF
                (-delta.x) > delta.y
                delta.x := -delta.y
            TRUE
                delta.y := -delta.x
        TRUE
        IF
            (-delta.x)>(-delta.y)
            delta.x := delta.y
        TRUE
            delta.y := delta.x
    l.x := n.x
    l.y := n.y
    to.graph ! c.draw.rectangle;
    m.x; m.y; delta.x; delta.y
    from.graph ? reply
    to.graph ! c.show.cursor
    from.graph ? reply
    TRUE
    SKIP

--- order the screen coordinates for
--- proper range
l.x := m.x + delta.x
IF
    m.x > l.x
    SEQ
        n.x := m.x
        m.x := l.x
        l.x := n.x
    TRUE
    SKIP
l.y := m.y + delta.y
IF
    m.y > l.y
    SEQ
        n.y := m.y
        m.y := l.y
        l.y := n.y
    TRUE
    SKIP

```

```
    select.ok := (delta.x <> 0) AND
                  (delta.y <> 0)

    --- right mouse button hit, do zoom in
    m.r AND select.ok
    SEQ
        done.select := TRUE
        graph.results ! zoom.in; m.x; m.y;
                        l.x; l.y

    --- left mouse button hit, do zoom out
    m.l AND select.ok
    SEQ
        done.select := TRUE
        graph.results ! zoom.out; m.x; m.y;
                        l.x; l.y

    TRUE
    SKIP
:
```

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